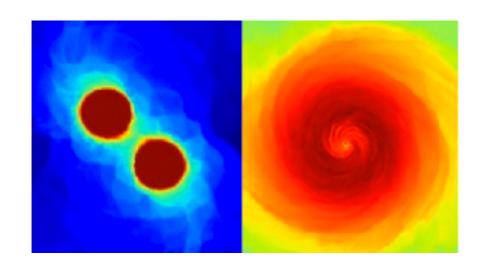
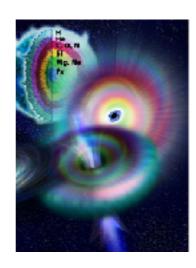
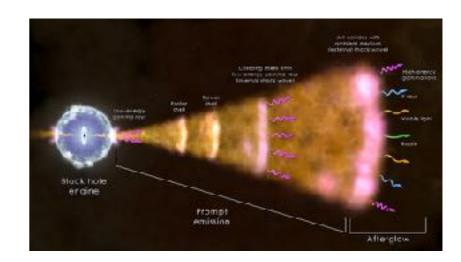


ICTP school: GRB afterglows slides





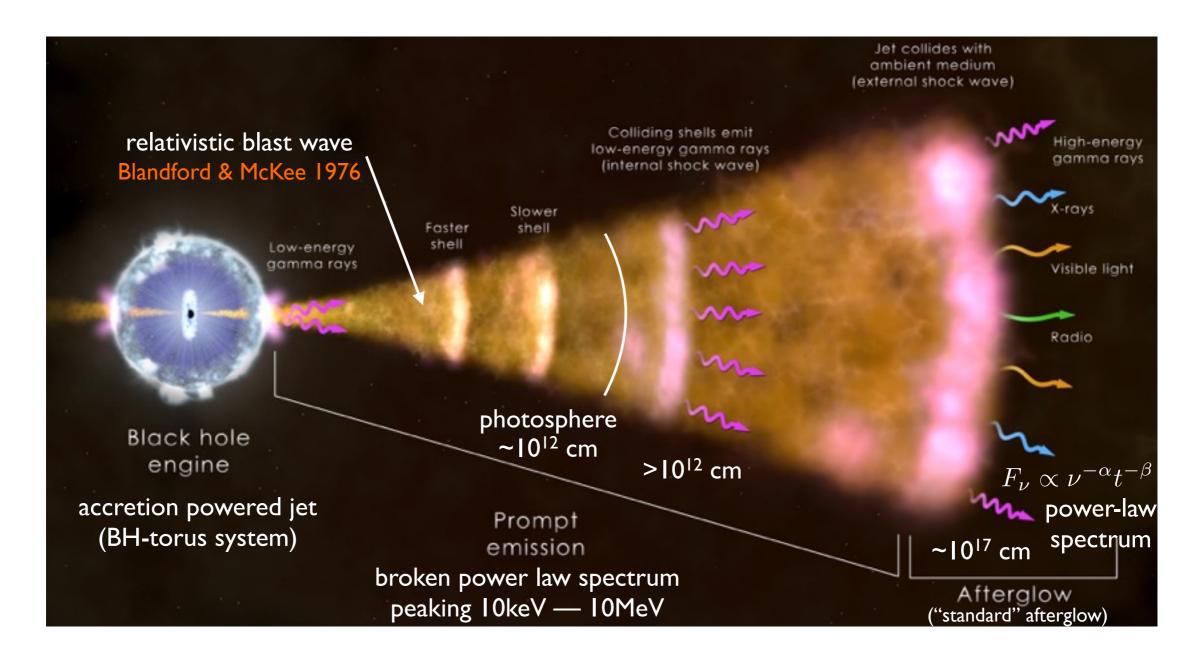


Daniel M. Siegel

Center for Theoretical Physics & Columbia Astrophysics Laboratory
Columbia University

ICTP school The Sound of Space-time: The Dawn of Gravitational Wave Science, Sao Paulo, Dec 10-14, 2018

The canonical GRB picture



How does the relativistic blast wave give rise to observable emission?

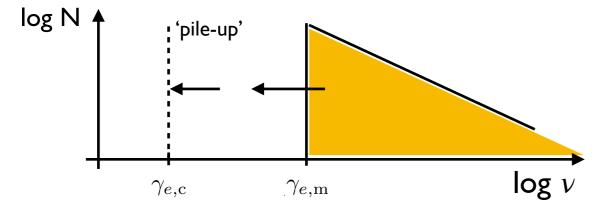
Daniel Siegel

Synchrotron afterglow spectrum

Two regimes:

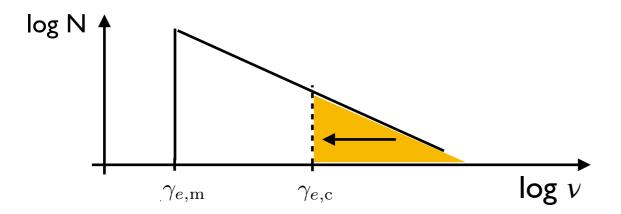
fast cooling $(\gamma_{e,m} > \gamma_{e,c})$

$$F_{\nu,\text{tot}} = \begin{cases} (\nu/\nu_{\text{c}})^{1/3} F_{\nu,\text{max}}, & \nu < \nu_{\text{c}} \\ (\nu/\nu_{\text{c}})^{-1/2} F_{\nu,\text{max}}, & \nu_{\text{c}} < \nu < \nu_{\text{m}} \\ (\nu/\nu_{\text{m}})^{-p/2} (\nu_{\text{m}}/\nu_{\text{c}})^{-1/2} F_{\nu,\text{max}}, & \nu > \nu_{\text{m}} \end{cases}$$

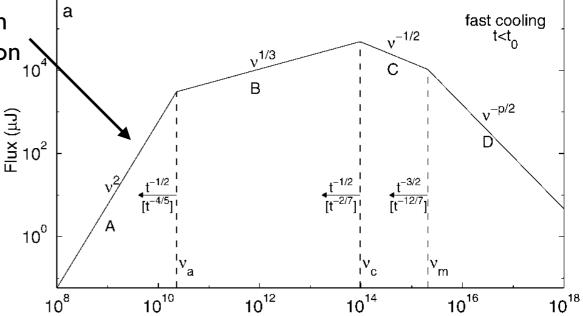


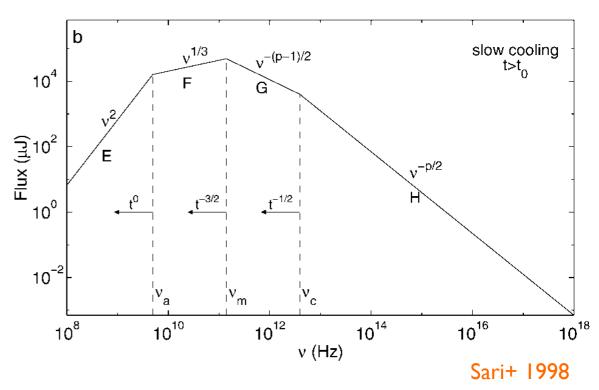
slow cooling $(\gamma_{e,m} < \gamma_{e,c})$

$$F_{\nu,\text{tot}} = \begin{cases} (\nu/\nu_{\text{m}})^{1/3} F_{\nu,\text{max}}, & \nu < \nu_{\text{m}} \\ (\nu/\nu_{\text{m}})^{-(p-1)/2} F_{\nu,\text{max}}, & \nu_{\text{m}} < \nu < \nu_{\text{c}} \\ (\nu/\nu_{\text{c}})^{-p/2} (\nu_{\text{c}}/\nu_{\text{m}})^{-(p-1)/2} F_{\nu,\text{max}}, & \nu > \nu_{\text{c}} \end{cases}$$



Synchrotron self-absorption \(\frac{10}{10} \)





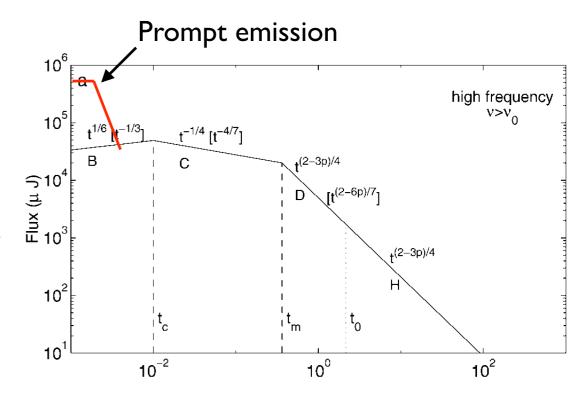
$$F_{\nu,\text{max}} = \frac{1}{4\pi D^2} N_e P_{\nu,\text{max}} = \frac{m_e c^3 \sigma_{\text{T}}}{9e} (32\pi m_{\text{p}})^{1/2} \epsilon_B^{1/2} n^{3/2} \gamma^2 R^3 D^{-2}$$

Synchrotron afterglow lightcurves

Two scenarios:

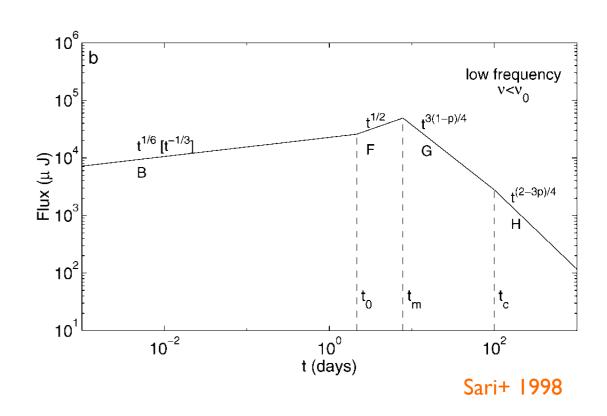
High-frequency lightcurve: $\nu_{\rm obs} > \nu_0$

$$L \simeq \nu_{\rm obs} F_{\nu, \rm tot}(\nu_{\rm obs}) \propto \begin{cases} \nu_{\rm c}^{-1/3}, & \propto t^{1/6}, & t < t_{\rm c} \\ \nu_{\rm c}^{1/2}, & \propto t^{-1/4}, & t_{\rm c} < t < t_{\rm m} \\ \nu_{\rm c}^{1/2} \nu_{\rm m}^{(p-1)/2}, & \propto t^{-(3p-2)/4}, & t > t_{\rm m} \end{cases}$$



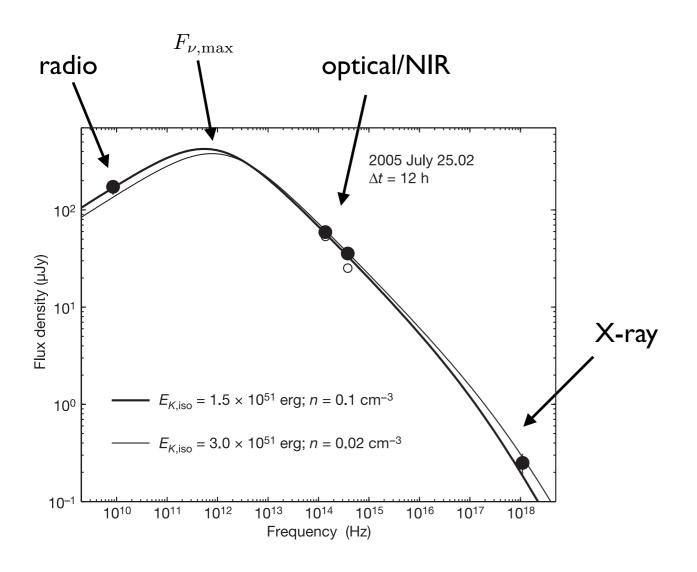
Low-frequency lightcurve: $\nu_{\rm obs} < \nu_0$

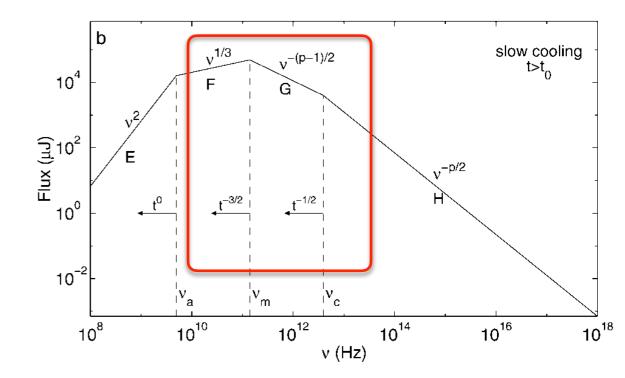
$$L \simeq \nu_{\rm obs} F_{\nu, \rm tot}(\nu_{\rm obs}) \propto \begin{cases} \nu_{\rm c}^{-1/3}, & \propto t^{1/6}, & t < t_0 \\ \nu_{\rm m}^{-1/3}, & \propto t^{1/2}, & t_0 < t < t_{\rm m} \\ \nu_{\rm m}^{(p-1)/2}, & \propto t^{-3(p-1)/4}, & t_{\rm m} < t < t_{\rm c} \\ \nu_{\rm m}^{(p-1)/2} \nu_{\rm c}^{1/2}, & \propto t^{-(3p-2)/4}, & t > t_{\rm c} \end{cases}$$



Afterglow spectrum of GRB 050724

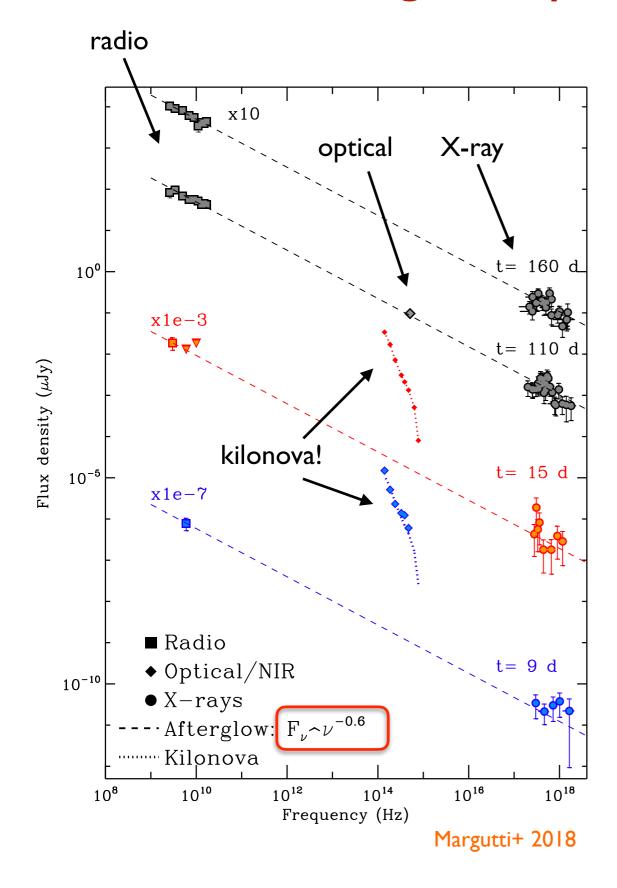
First observed short GRB with detected radio+optical/NIR+X-ray afterglow

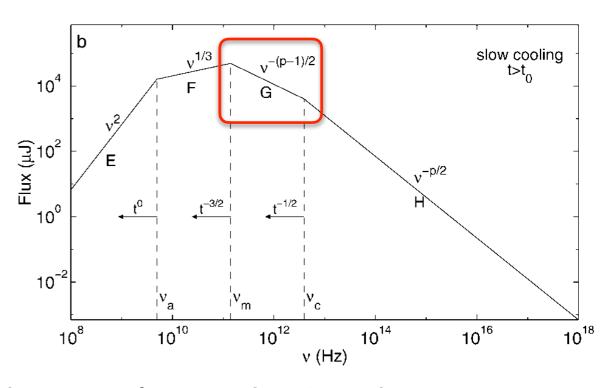




Berger+ 2005, Nature

Afterglow spectrum of GW170817





 perfect power-law over 9 orders of magnitude in frequency!

 $\nu_{\rm c}$ above X-rays

 $\nu_{
m m}$ below radio

→ slow-cooling regime

$$(p-1)/2 = 0.6 \implies p = 2.2$$

• other inferred parameters:

$$E \sim 5 \times 10^{50} \,\mathrm{erg}, \ n \sim 10^{-4} \,\mathrm{cm}^{-3}, \ \epsilon_e = 0.02, \ \epsilon_B = 0.001$$